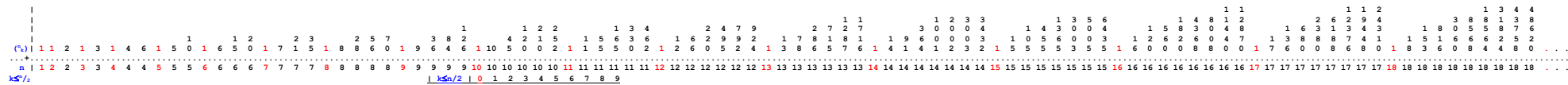


The Binomial Slide Rule by István Szalkai, Veszprém, Hungary, szalkai@almos.uni-pannon.hu , 2017.05.24.

<http://math.uni-pannon.hu/~szalkai/Binom-lec4.docx> ,

<http://math.uni-pannon.hu/~szalkai/Binom-lec4.pdf>



Description and use

The **binomial coefficients** $\binom{n}{k} := \frac{n(n-1)\dots(n-k+1)}{k!}$ are defined for all natural numbers $n, k \in \mathbb{N}$, $0 \leq k \leq n$.

By the *symmetry property* $\binom{n}{k} = \binom{n}{n-k}$ we have to compute their values only for $0 \leq k \leq n/2$.

The slide rule above contains *three scales*: the scales denoted by " $\binom{n}{k}$ " and by " n " are on the stator, the third one (below the dotted line), denoted by " $k \leq n/2$ " is on the slide. The digits of the numbers on the *first scale* are printed *vertically*, e.g. the three digits 1, 2, 6 above the last 9 (just before the red 10) represent the number 126.

To compute $\binom{n}{k}$ choose first n , say 10. Move the slide (scale " $k \leq n/2$ ") so that the 0 sign on it would be exactly under the *first*, red 10 sign of scale " n ", as it shown now on the slide rule. Now you can read the values $\binom{10}{k}$ above, on the top scale " $\binom{n}{k}$ " as: $\binom{10}{0} = \binom{10}{10} = 1$, $\binom{10}{1} = \binom{10}{9} = 10$, $\binom{10}{2} = \binom{10}{8} = 45$, $\binom{10}{3} = \binom{10}{7} = 120$, $\binom{10}{4} = \binom{10}{6} = 210$ and $\binom{10}{5} = 252$. You may also imagine brackets around the figures on scales " n " and " $\binom{n}{k}$ " to see " $\binom{10}{k}$ " printed on the slide rule. (Clearly you can *not* use values of k under the next (red or black) $n+1$, i.e. for $k > n/2$.)

When using a text editor, you are able to *move* the slide with scale " $k \leq n/2$ " by deleting/inserting spaces from/to the line " $k \leq n/2$ " (since the font used is not proportional).

Further, using smaller font size the above slide rule can be extended for n larger than 18.

Have a nice time, and let me know any comment you have!

István